

UNIVERSITI SAINS MALAYSIA

Peperiksaan Semester Tambahan  
Sidang 1988/89

Jun 1989

**EBB 218 Proses-proses Pengangkutan**

Masa : [3 jam]

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**ARAHAN KEPADA CALON**

1. Sila pastikan bahawa kertas peperiksaan ini mengandungi SEPULUH muka surat bercetak sebelum anda memulakan peperiksaan ini.
2. Jawab LIMA soalan sahaja.
3. Jawapan untuk setiap soalan MESTI dimulakan pada muka surat yang berasingan.
4. Semua jawapan MESTILAH dijawab di dalam Bahasa Malaysia.
5. Kertas soalan ini mengandungi ENAM soalan.

1. a) Bagi aliran laminar di antara dua plat selari jarak  $z$ , tunjukkan bahawa kadar alir  $Q$  boleh diungkapkan sebagai berikut dengan menggunakan persamaan Navier Stoke. Lihat lampiran 1.

$$Q = \frac{-1}{\eta} \frac{dp}{dz} \frac{z^3}{12} + \frac{z}{2} (U + V)$$

$\eta$  adalah kelikatan dinamik bendalir,  $\frac{dp}{dz}$  adalah kecerunan tekanan diarah alir,  $U$  adalah halaju plat atas dan  $V$  adalah halaju plat bawah.

(60 markah)

- b) Ketumpatan bendalir adalah  $1260 \text{ kg/m}^3$  dan kelikatan  $0.9 \text{ Ns/m}^2$  mengalir di antara dua plat selari jarak  $2 \text{ cm}$ . Jika kadar alir adalah  $0.5 \text{ litre/saat}$  per lebar, kirakan susutan tekanan per unit panjang jika kedua-dua plat pegun. Tentukan halaju purata. Tunjukkan bahawa halaju purata adalah  $\frac{2}{3}$  halaju maksimum.

(40 markah)

2. a) Tunjukkan formula Darcy boleh diungkapkan seperti berikut berdasarkan persamaan pergerakan.

$$h_f = \frac{4fv^2L}{2dg}$$

(30 markah)

- b) Minyak, graviti tentu  $0.9$  dan kelikatan kinematik  $0.00001 \text{ m}^2/\text{s}$  mengalir pada  $2 \text{ m}^3/\text{s}$  melalui paip panjang  $500 \text{ m}$  dan garispusat  $200 \text{ mm}$ . Relatif kekasaran bagi paip besi tuang adalah  $0.0013$ .

a) Tentukan kehilangan turus akibat geseran

b) Susutan tekanan jika paip condong  $10^\circ$  dari mendatar.

(70 markah)

3. a) Berdasarkan aliran haba ke dalam unsur kecil, buktikan bahawa persamaan Poisson keselantaran aliran haba bagi sistem koordinat segi empat adalah seperti berikut.

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} + \frac{q''}{k} = 0$$

$q'' \equiv$  Penjanaan haba dalaman

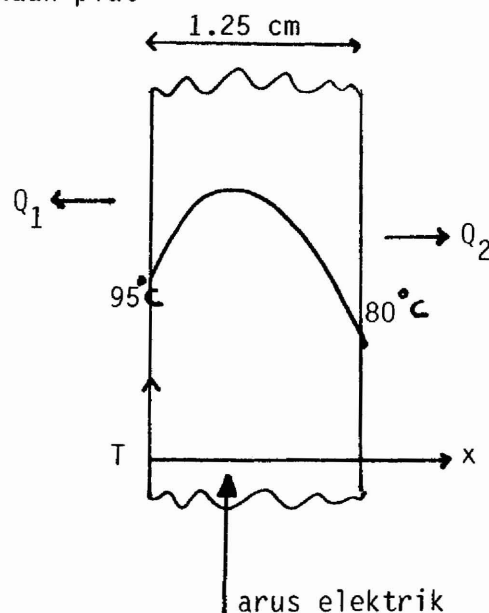
$k \equiv$  Pekali keberkondukan

(30 markah)

- b) Timbangkan pengaliran satu dimensi dengan penjanaan haba melalui plat keluli. Tebal plat adalah 1.25 cm, lebarnya 10 cm dan panjangnya tak terhingga.

Arus elektrik mengalir sepanjang plat keluli dan menjanakan haba 88780 kW/m<sup>2</sup>. Suhu permukaan plat adalah 80°C dan 95°C. Lihat Rajah 1. Pekali keberkondukan adalah 54 W/mK.

- i) Dapatkan persamaan taburan suhu
- ii) Tentukan nilai suhu maksimum dan kedudukannya.
- iii) Kadar alir per unit panjang  $Q_1$  dan  $Q_2$  (kW/m) daripada permukaan plat



(70 markah)

4. a) Dengan menggunakan teorem  $\pi$  Buckingham, tunjukkan bahawa bagi permindahan haba olakan bebas

$$Nu = f(Gr, Pr)$$

$$Nu \equiv \text{No Nusselt} \quad \frac{hd}{k}$$

$$Gr \equiv \text{No Grashof} \quad \frac{\beta g \rho^2 d^3 \Delta T}{\eta^2}$$

$$Pr \equiv \text{No Prandtl} \quad \frac{\eta C}{k}$$

$h$   $\equiv$  pekali permindahan haba

$d$   $\equiv$  garispusat tiub

$k$   $\equiv$  pekali keberkondukan bendalir

$\rho$   $\equiv$  ketumpatan bendalir

$\eta$   $\equiv$  kelikatan bendalir

$C$   $\equiv$  muatan haba

$\beta$   $\equiv$  pekali pengembangan

$T$   $\equiv$  suhu

$g$   $\equiv$  pecutan graviti

(40 markah)

- b) Sebatang silinder mendatar mempunyai garispusat 8 cm dan terdedah kepada udara pegun pada suhu 400 K dan tekanan 1 atmosfera. Suhu permukaan silinder adalah 500 K. Tentukan kehilangan haba per unit panjang silinder.

Data bagi sifat udara boleh ditentukan daripada lampiran 2.

(60 markah)

5. a) Secara ringkas terangkan mekanisme resapan berikut;

- i) Resapan kekosongan
- ii) Resapan gelang
- iii) Resapan kecelahan
- iv) Resapan celahan

(30 markah)

- b) Sekeping keluli karbon setebal 1 mm mempunyai 0.2% berat karbon. Proses penyahkarbonan mengkehendaki 0.1% berat karbon di bahagian satu pertiga daripada permukaan.

Berikan tiga kombinasi masa rawatan dan suhu rawatan bagi proses ini dengan menggunakan jeda suhu yang berpatutan.

Malar resapan untuk karbon di dalam keluli adalah seperti berikut:

$$A = 2 \times 10^{-5} \text{ m}^2/\text{s}$$

$$Q = 145 \text{ kJ/mol}$$

$$R = 8.31 \text{ J/K mol}$$

$$\text{Berat atom karbon} = 12.0$$

$$\text{Berat atom besi} = 55.8$$

Persamaan untuk sistem resapan tidak tak terhingga adalah

$$C_x = \frac{4C_0}{\pi} \sum_{j=0}^{\infty} \frac{1}{2j+1} \sin \left( (2j+1) \frac{\pi x}{\Delta x} \right) \exp \left[ - \left( \frac{(2j+1)\pi}{\Delta x} \right)^2 Dt \right]$$

(70 markah)

6. a) Dengan menggunakan teorem  $\pi$  Buckingham buktikan bahawa bagi pengangkutan jisim dengan olakan paksa

$$Sh = f(Re, Sc)$$

$$Sh = \text{No sherwood } \frac{kx}{D}$$

$$Re = \frac{\rho v x}{\eta}$$

$$Sc = \eta / \rho D$$

$k$  = pekali permindahan jisim

$D$  = pekali resapan

$x$  = jarak

$\rho$  = ketumpatan bendalir

$v$  = halaju

$\eta$  = kelikatan bendalir

(40 markah)

- b) Bagi lapisan sempadan laminar

$$Sh = 0.332 Re_x^{1/2} Sc^{1/3}$$

dan bagi lapisan sempadan gelora

$$Sh = 0.0292 Re_x^{4/5} Sc^{1/3}$$

Peralihan dariapda laminar ke gelora berlaku apabila  $Re_t = 3 \times 10^5$

Bagi  $Sc = 1.2$ ,  $Re = 1 \times 10^6$ , panjang plat 2 meter dan pekali resapan

$D = 1.3 \times 10^{-5} \text{ m}^2/\text{s}$ , tentukan pekali permindahan jisim purata.

(60 markah)

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TABLE 3.4-2  
THE EQUATION OF MOTION IN RECTANGULAR COORDINATES ( $x, y, z$ )

In terms of  $\tau$ :

$$\begin{aligned} x\text{-component} \quad \rho \left( \frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \right) = & - \frac{\partial p}{\partial x} \\ & - \left( \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{yx}}{\partial y} + \frac{\partial \tau_{zx}}{\partial z} \right) + \rho g_x \quad (A) \end{aligned}$$

$$\begin{aligned} y\text{-component} \quad \rho \left( \frac{\partial v_y}{\partial t} + v_x \frac{\partial v_y}{\partial x} + v_y \frac{\partial v_y}{\partial y} + v_z \frac{\partial v_y}{\partial z} \right) = & - \frac{\partial p}{\partial y} \\ & - \left( \frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{zy}}{\partial z} \right) + \rho g_y \quad (B) \end{aligned}$$

$$\begin{aligned} z\text{-component} \quad \rho \left( \frac{\partial v_z}{\partial t} + v_x \frac{\partial v_z}{\partial x} + v_y \frac{\partial v_z}{\partial y} + v_z \frac{\partial v_z}{\partial z} \right) = & - \frac{\partial p}{\partial z} \\ & - \left( \frac{\partial \tau_{xz}}{\partial x} + \frac{\partial \tau_{yz}}{\partial y} + \frac{\partial \tau_{zz}}{\partial z} \right) + \rho g_z \quad (C) \end{aligned}$$

In terms of velocity gradients for a Newtonian fluid with constant  $\rho$  and  $\mu$ :

$$\begin{aligned} x\text{-component} \quad \rho \left( \frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \right) = & - \frac{\partial p}{\partial x} \\ & + \mu \left( \frac{\partial^2 v_x}{\partial x^2} + \frac{\partial^2 v_x}{\partial y^2} + \frac{\partial^2 v_x}{\partial z^2} \right) + \rho g_x \quad (D) \end{aligned}$$

$$\begin{aligned} y\text{-component} \quad \rho \left( \frac{\partial v_y}{\partial t} + v_x \frac{\partial v_y}{\partial x} + v_y \frac{\partial v_y}{\partial y} + v_z \frac{\partial v_y}{\partial z} \right) = & - \frac{\partial p}{\partial y} \\ & + \mu \left( \frac{\partial^2 v_y}{\partial x^2} + \frac{\partial^2 v_y}{\partial y^2} + \frac{\partial^2 v_y}{\partial z^2} \right) + \rho g_y \quad (E) \end{aligned}$$

$$\begin{aligned} z\text{-component} \quad \rho \left( \frac{\partial v_z}{\partial t} + v_x \frac{\partial v_z}{\partial x} + v_y \frac{\partial v_z}{\partial y} + v_z \frac{\partial v_z}{\partial z} \right) = & - \frac{\partial p}{\partial z} \\ & + \mu \left( \frac{\partial^2 v_z}{\partial x^2} + \frac{\partial^2 v_z}{\partial y^2} + \frac{\partial^2 v_z}{\partial z^2} \right) + \rho g_z \quad (F) \end{aligned}$$

## The Equations of Change in Curvilinear Coordinates

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TABLE 3.4-3  
THE EQUATION OF MOTION IN CYLINDRICAL COORDINATES  $(r, \theta, z)$

In terms of  $\tau$ :

$$\begin{aligned} r\text{-component}^a \quad \rho \left( \frac{\partial v_r}{\partial t} + v_r \frac{\partial v_r}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_r}{\partial \theta} - \frac{v_\theta^2}{r} + v_z \frac{\partial v_r}{\partial z} \right) = & - \frac{\partial p}{\partial r} \\ & - \left( \frac{1}{r} \frac{\partial}{\partial r} (r \tau_{rr}) + \frac{1}{r} \frac{\partial \tau_{r\theta}}{\partial \theta} - \frac{\tau_{\theta\theta}}{r} + \frac{\partial \tau_{rz}}{\partial z} \right) + \rho g_r \quad (A) \end{aligned}$$

$$\begin{aligned} \theta\text{-component}^b \quad \rho \left( \frac{\partial v_\theta}{\partial t} + v_r \frac{\partial v_\theta}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_\theta}{\partial \theta} + \frac{v_r v_\theta}{r} + v_z \frac{\partial v_\theta}{\partial z} \right) = & - \frac{1}{r} \frac{\partial p}{\partial \theta} \\ & - \left( \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \tau_{r\theta}) + \frac{1}{r} \frac{\partial \tau_{\theta\theta}}{\partial \theta} + \frac{\partial \tau_{\theta z}}{\partial z} \right) + \rho g_\theta \quad (B) \end{aligned}$$

$$\begin{aligned} z\text{-component} \quad \rho \left( \frac{\partial v_z}{\partial t} + v_r \frac{\partial v_z}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_z}{\partial \theta} + v_z \frac{\partial v_z}{\partial z} \right) = & - \frac{\partial p}{\partial z} \\ & - \left( \frac{1}{r} \frac{\partial}{\partial r} (r \tau_{rz}) + \frac{1}{r} \frac{\partial \tau_{\theta z}}{\partial \theta} + \frac{\partial \tau_{zz}}{\partial z} \right) + \rho g_z \quad (C) \end{aligned}$$

In terms of velocity gradients for a Newtonian fluid with constant  $\rho$  and  $\mu$ :

$$\begin{aligned} r\text{-component}^a \quad \rho \left( \frac{\partial v_r}{\partial t} + v_r \frac{\partial v_r}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_r}{\partial \theta} - \frac{v_\theta^2}{r} + v_z \frac{\partial v_r}{\partial z} \right) = & - \frac{\partial p}{\partial r} \\ & + \mu \left[ \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial}{\partial r} (r v_r) \right) + \frac{1}{r^2} \frac{\partial^2 v_r}{\partial \theta^2} - \frac{2}{r^2} \frac{\partial v_\theta}{\partial \theta} + \frac{\partial^2 v_r}{\partial z^2} \right] + \rho g_r \quad (D) \end{aligned}$$

$$\begin{aligned} \theta\text{-component}^b \quad \rho \left( \frac{\partial v_\theta}{\partial t} + v_r \frac{\partial v_\theta}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_\theta}{\partial \theta} + \frac{v_r v_\theta}{r} + v_z \frac{\partial v_\theta}{\partial z} \right) = & - \frac{1}{r} \frac{\partial p}{\partial \theta} \\ & + \mu \left[ \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial}{\partial r} (r v_\theta) \right) + \frac{1}{r^2} \frac{\partial^2 v_\theta}{\partial \theta^2} + \frac{2}{r^2} \frac{\partial v_r}{\partial \theta} + \frac{\partial^2 v_\theta}{\partial z^2} \right] + \rho g_\theta \quad (E) \end{aligned}$$

$$\begin{aligned} z\text{-component} \quad \rho \left( \frac{\partial v_z}{\partial t} + v_r \frac{\partial v_z}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_z}{\partial \theta} + v_z \frac{\partial v_z}{\partial z} \right) = & - \frac{\partial p}{\partial z} \\ & + \mu \left[ \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial v_z}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 v_z}{\partial \theta^2} + \frac{\partial^2 v_z}{\partial z^2} \right] + \rho g_z \quad (F) \end{aligned}$$



**TABLE B-3**  
PROPERTIES OF AIR  
AT ATMOSPHERIC  
PRESSURE

The values of  $\mu$ ,  $k$ ,  $c_p$ , and  $Pr$  are not strongly pressure-dependent and may be used over a fairly wide range of pressures.

$T$ , K	$\rho$ , kg/m <sup>3</sup>	$c_p$ , kJ/ kg·°C	$\mu$ , kg/m·s $\times 10^5$	$\nu$ , m <sup>2</sup> /s $\times 10^6$	$k$ , W/ m·°C	$\alpha$ , m <sup>2</sup> /s $\times 10^4$	$Pr$
100	3.6010	1.0266	0.6924	1.923	0.009 246	0.025 01	0.770
150	2.3675	1.0099	1.0283	4.343	0.013 735	0.057 45	0.753
200	1.7684	1.0061	1.3289	7.490	0.01809	0.101 65	0.739
250	1.4128	1.0053	1.5990	11.31	0.02227	0.156 75	0.722
300	1.1774	1.0057	1.8462	15.69	0.02624	0.221 60	0.708
350	0.9980	1.0090	2.075	20.76	0.03003	0.2983	0.697
400	0.8826	1.0140	2.286	25.90	0.03365	0.3760	0.689
450	0.7833	1.0207	2.484	31.71	0.03707	0.4222	0.683
500	0.7048	1.0295	2.671	37.90	0.04038	0.5564	0.680
550	0.6423	1.0392	2.848	44.34	0.04360	0.6532	0.680
600	0.5879	1.0551	3.018	51.34	0.04659	0.7512	0.680
650	0.5430	1.0635	3.177	58.51	0.04953	0.8578	0.682
700	0.5030	1.0752	3.332	66.25	0.05230	0.9672	0.684
750	0.4709	1.0856	3.481	73.91	0.05509	1.0774	0.686
800	0.4405	1.0978	3.625	82.29	0.05779	1.1951	0.689
850	0.4149	1.1095	3.765	90.75	0.06028	1.3097	0.692
900	0.3925	1.1212	3.899	99.3	0.06279	1.4271	0.696
950	0.3716	1.1321	4.023	108.2	0.06525	1.5510	0.699
1000	0.3524	1.1417	4.152	117.8	0.06752	1.6779	0.702
1100	0.3204	1.160	4.44	138.6	0.0732	1.969	0.704
1200	0.2947	1.179	4.69	159.1	0.0782	2.251	0.707
1300	0.2707	1.197	4.93	182.1	0.0837	2.583	0.705
1400	0.2515	1.214	5.17	205.5	0.0891	2.920	0.705
1500	0.2355	1.230	5.40	229.1	0.0946	3.262	0.705
1600	0.2211	1.248	5.63	254.5	0.100	3.609	0.705
1700	0.2082	1.267	5.85	280.5	0.105	3.977	0.705
1800	0.1970	1.287	6.07	308.1	0.111	4.379	0.704
1900	0.1858	1.309	6.29	338.5	0.117	4.811	0.704
2000	0.1762	1.338	6.50	369.0	0.124	5.260	0.702
2100	0.1682	1.372	6.72	399.6	0.131	5.715	0.700
2200	0.1602	1.419	6.93	432.6	0.139	6.120	0.707
2300	0.1538	1.482	7.14	464.0	0.149	6.540	0.710
2400	0.1458	1.574	7.35	504.0	0.161	7.020	0.718
2500	0.1394	1.688	7.57	543.5	0.175	7.441	0.730

Source: From Natl. Bur. Stand. (U.S.) Circ. 564, 1955.

TABLE 11-6  
Convection Heat-  
Transfer Correlations  
for Free Convection,  
Constant Surface  
Temperature

General relation: $\overline{Nu} = C(GrPr)^m$ with properties evaluated at film temperature			
	$GrPr$	$C$	$m$
Vertical planes and cylinders	$10^4-10^9$	0.59	1/4
	$10^9-10^{13}$	0.10	1/3
Horizontal cylinders	$10^{-10}-10^{-2}$	0.675	0.058
	$10^{-2}-10^2$	1.02	0.148
	$10^2-10^4$	0.85	0.188
	$10^4-10^9$	0.53	1/4
	$10^9-10^{12}$	0.13	1/3
Upper surface of heated plates or lower surface of cooled plates	$2 \times 10^4-8 \times 10^6$	0.54	1/4
Upper surface of heated plates or lower surface of cooled plates	$8 \times 10^6-10^{11}$	0.15	1/3
Lower surface of heated plates or upper surface of cooled plates	$10^5-10^{11}$	0.58	1/5

